

# REDUCTION OF MOIRÉ EFFECT IN PIXELATED REAR-PROJECTION DISPLAYS

## FIELD OF THE INVENTION

The present invention relates to projection displays  
5 and more specifically to reducing the moiré effect  
associated with rear-projection displays based on  
pixelated technologies, such as DMD, LCD, LCOS, etc.

## BACKGROUND OF THE INVENTION

The typical screen technology in rear projection  
10 displays utilizes a special dark-stripe structure to  
improve the ambient light rejection, which effectively  
provides a higher contrast display. This dark-stripe  
structure is simply an array of blackened vertical  
stripes, separated by regions allowing light to pass  
15 through. These regions allowing light to pass through,  
whether they may be transparent, translucent, diffuse, or  
another type of structure, will be referred to herein as  
clear stripes or simply stripes or structures allowing  
light to pass. For CRT based displays these screens work  
20 fine. However for pixelated (digital) displays, which  
utilize digital spatial light modulators (SLM) such as  
the micromirror device (DMD) or LCD technology, the  
current dark-stripe structure can interfere optically  
with the pixelated structure of the SLMs, causing  
25 interference fringes known as moiré patterns.

FIGURES 1a and 1b are top and front drawings, respectively, of a typical dark-stripe, or dark-stripe rear-projection screen. The backside of the screen, where the projected image enters, consists of a layer of small lenticular lens elements 10. The dark-stripe structure is fabricated on the opposite surface (from the lens elements) of the lenticular layer and consists of vertical black stripes 11 separated by transparent (clear) stripes 12. Next, a diffusion layer 13 is put on top of the dark-stripe layer to diffuse the light 15, coming through the transparent stripes 12, across the entire screen 150-154. Finally a hard coating layer 14 is applied on the outside surface of the screen for protection purposes.

In operation, the black stripes 11 tend to make the screen look dark to the viewer while still letting light pass through it. This provides adequate picture contrast for viewing in a room with ordinary lighting conditions (although not intended for use in direct sunlight).

In these display screens, the lenticular lens elements 10 are optimized to direct most of the available light to a viewing spot directly in front of the screen, where a typical viewer is likely to be located. As the viewer moves away from this central viewing point, either

vertically or horizontally, the brightness will gradually decrease.

FIGURE 2a is a Fourier transform of a continuous-time signal and FIGURES 2a and 2b are Fourier transforms of discrete-time signals obtained by periodic sampling this continuous signal, which illustrate what causes the moiré fringes in digital displays. In FIGURE 2b the sampling period for the screen is large (low sampling rate), so that the periodic repetitions of the continuous-time transform (FIGURE 2a) overlap. In this case, the upper frequencies in  $X_a(j\Omega)$  (FIGURE 2a) get reflected into the lower frequencies in  $X(e^{j\omega})$  (FIGURE 2b) in the overlapped areas. This phenomenon, where in effect the high frequency component in the continuous time signal takes on the identity of a lower frequency, is called aliasing and causes moiré fringes to occur. On the other hand, in FIGURE 2c the sampling period for the screen is small enough (high sampling rate) so that the periodic repetitions of the continuous time transform do not overlap and therefore moiré fringes do not occur.

FIGURE 3 is an example of the moiré effect 32. This illustration involves overlaying one pixelated pattern 31 over a second pixelated pattern 30 and slightly rotating the patterns relative to each other to establish the overlapping conditions discussed in FIGURE 2b.

The pitch (spacing between lines) of dark-stripe screens is continuously getting smaller as screen technology advances, but so are the display pixels, so that moiré effects will continue to be a problem. What  
5 is needed is a method to provide a step-function improvement to overcome this problem. The disclosed invention accomplishes this by rotating the dark-stripe structure relative to the displayed pixels.

## SUMMARY OF THE INVENTION

This invention discloses a method for reducing the moiré effect in rear-projection displays by rotating the dark-stripe structure in the screen  $45 \pm 15$  degrees relative to the vertical axis of the display. By rotating the black stripes relative to the display pixels, the spatial frequency at which the moiré effect sets in can be improved by 15% to 41%.

To prevent the moiré phenomenon from occurring, the Nyquist rate of the screen structure must be less than one-half the pixel rate (as imaged on the screen); that is, the projected pixel pitch is greater than twice the screen structure pitch. The method of this invention extends the ratio of the projected pixel pitch to screen structure pitch by a factor of up to 1.41.

The lenticular lens elements on the input surface of the screen can be shaped to match the angle of the opening between dark-stripes to maintain a high brightness level in the center of the screen that decreases in the normal sense as the viewer moves in either the vertical or horizontal directions, if desired.

This method extends the use of existing lower-cost dark-stripe screens to provide high performance displays with reduced moiré interference and as screen technology advances with finer dark-stripe pitch, will continue to

provide between 15% and 41% improvement over conventional vertical stripe screens.

#### BRIEF DESCRIPTION OF THE DRAWINGS

For a more complete understanding of the present  
5 invention, and the advantages thereof, reference is now made to the following descriptions taken in conjunction with the accompanying drawings, in which:

FIGURES 1a and 1b are drawings showing the top and front views of a conventional dark-stripe rear-projection  
10 display screen.

FIGURE 2a is a waveform for a Fourier transform of a continuous-time signal.

FIGURE 2b is a waveform for a Fourier transform of a discrete-time signal obtained by periodic sampling the  
15 continuous waveform of FIGURE 2a, for the case where the sampling period is large so that the periodic repetitions of the continuous-time transform overlap, resulting in a moiré fringes.

FIGURE 2c is a waveform for a Fourier transform of a  
20 discrete-time signal obtained by periodic sampling the continuous waveform of FIGURE 2a for the case where the sampling period is small enough that the periodic repetitions of the continuous-time transform do not overlap and therefore do not cause moiré fringes to  
25 occur.

FIGURE 3 is a sketch illustrating the moiré effect where one pixelated pattern is laid over a second pixelated pattern and slightly rotated to generate the moire fringe pattern.

5        FIGURES 4a and 4b are drawings showing the top and front views of the dark-stripe rear-projection screen of the present invention, where the dark-stripe structure is rotated  $45 \pm 15$  degrees relative to the pixels being displayed on the screen.

10       FIGURES 5a and 5b are drawings illustrating the pixel pitch vs. screen structure pitch for a conventional dark-stripe screen and the rotated dark-stripe screen of the present invention, respectively.

FIGURE 5c is a graph illustrating the trigonometric  
15    improvement in pixel pitch to dark-stripe pitch realized by rotating the dark-stripe structure in the method of the present invention.

FIGURES 6a and 6b show lenticular lens elements for the rotated dark-stripe screen of the present invention,  
20    where the lens elements are shaped to reduce the brightness roll-off along the horizontal screen axis.

FIGURE 7 is a drawing of a rear-projection display, which uses the rotated black-strip display screen of the present invention.

FIGURE 8 illustrates the pixel pitch vs. screen structure pitch for a conventional dark-stripe screen combined with an image produced by an array of diamond-shaped pixels.

5      FIGURE 9 illustrates the pixel pitch vs. screen structure pitch for a conventional dark-stripe screen combined with an image produced by a staggered pixel array.



## DETAILED DESCRIPTION OF THE PREFERRED EMBODIMENTS

This invention discloses a method for reducing the moiré effect in rear-projection displays by rotating the dark-stripe structure in the screen  $45 \pm 15$  degrees relative to the displayed pixels or the axes of the display. By rotating the dark-stripes relative to the displayed pixels, the spatial frequency at which the moiré effect sets in can be improved by 15% to 41%.

FIGURES 4a and 4b are drawings showing the top and front views of the dark-stripe rear-projection screen of the present invention, where the dark-stripe structure is rotated  $45 \pm 15$  degrees relative to the axes of the screen. The backside of the screen where the projected image enters, consists of a layer of small lenticular lens elements 40. The dark-stripe structure is fabricated on the opposite surface (from the lens elements) of the lenticular layer and consists of diagonal black stripes 41 separated by transparent (clear) stripes 42. However, in this case the dark-stripe structure is rotated from  $45 \pm 15$  degrees relative to the vertical axis of the screen. Next, a diffusion layer 43 is fabricated on top of the rotated dark-stripe layer to diffuse the light 45, coming through the transparent stripes 42, across the entire screen 450-454.

Finally a hard coating layer 44 is applied on the outside surface of the screen for protection purposes.

In operation, the rotated black stripes 41 tend to make the screen look dark to the viewer while still  
5 letting light pass through it. This provides adequate picture contrast for viewing in a room having ordinary lighting conditions.

In these display screens the lenticular lens elements 40 are optimized to direct most of the available  
10 light to a viewing spot directly in front of the screen, where a typical viewer is likely to be located. However, in this case the maximum roll-off in brightness will occur as the viewer moves away from this central viewing point in a diagonally manner. Although this has proven  
15 to be acceptable, the lenticular lens elements can be shaped to cause the maximum brightness roll-off to occur in the vertical and horizontal directions, if desired.

To prevent moiré patterns from occurring in dark-stripe rear-projection screens the conditions stated in  
20 the following equation must exist:

Projected Pixel Pitch  $\geq$  2x Screen Structure Pitch,  
where screen structure pitch is defined as the distance between black stripes on the screen and projected pixel pitch as the distance between the  
25 projector's pixels as imaged on the screen.

Another way of saying this is that since the screen pitch must be  $\leq$  one-half the projected pixel pitch, then the sampling rate ( $1/\text{pitch}$ ) of the screen, generally referred to as the Nyquist rate, must be  $\geq 2$  the projected pixel rate.

FIGURES 5a and 5b are drawings illustrating the projected pixel pitch vs. screen structure pitch for a conventional dark-stripe screen and the rotated dark-stripe screen of the present invention, respectively. In FIGURE 5a, the projector's pixels are defined by the dark lines 50, while the screen's dark-stripe structure is shown by the shaded/white columns 52/53. In this drawing, the projected pixel pitch 51 is 2 times the dark-stripe pitch 54; e.g., the projected pixel pitch 51 may be 1 mm and the dark-stripe pitch 54 0.5 mm.

Therefore, the screen sampling rate is 2 times the pixel sampling rate, thereby just satisfying the Nyquist rate so that moiré patterns would not be introduced. However, since the pixel pitch of many newer Spatial Light Modulators is being reduced, the impact of moiré using the same dark-stripe screen may increase and become objectionable. As the screen's dark-stripe structure is made finer as in the case of future more expensive screens, there is greater margin before the Nyquist rate is exceeded and moiré effects become evident.

However, as shown in FIGURE 5b the Nyquist rate can be improved for the same black-strip screen of FIGURE 5a by rotating the dark-stripe structure relative to the displayed pixels. In this example, the pixels are  
5 defined by the dark lines 55 and the dark-stripe structure by diagonal shaded/white stripes 57/58, which is rotated  $45^\circ$  relative to the pixels. The dark-stripe pitch 59 is the same (0.5 mm) as in the earlier example, but the pixel pitch 56 is now 1.4 mm, or 41% greater than  
10 for the vertical stripe example. This means that a given screen has up to a 41% greater margin against moiré effects, for the rotated dark-stripe structure of the present invention, over the conventional vertical dark-stripe structure.

15 FIGURE 5c is a graph showing the trigonometric relationship realized by rotating the dark-stripe structure in a rear-projection screen. In this graph, the length of lines 500, 501 represents the pixel pitch for a conventional vertical dark-stripe screen, while the  
20 length of lines 510, 520, and 530 represent the effective pixel pitch for the rotated dark-stripe screen of the present invention, where the structure is rotated  $30^\circ$  5100 and  $45^\circ$  5200 relative to the vertical axis or  $30^\circ$  5300 and  $45^\circ$  5201 relative to the horizontal axis.

Normalizing the length of these vectors so that lines  
500,501 for a conventional screen is 1.0, then the length  
of lines 510, 520, and 530 for the rotated dark-stripe  
structure of the present invention are 1.15, 1.41, and  
5 1.15, respectively. This represents a maximum improvement  
in the Nyquist rate of 41% when the dark-stripe structure  
57 is rotated 45° and 15% when rotated 30° relative to  
either the vertical or the horizontal axis of the screen.

The trigonometric functions to establish this  
10 improvement is given as follows:

For rotations of 30 to 45 degrees from the vertical  
axis of the screen,

$\cosine(\theta) = L(500) / L(\theta)$  , so that for

$L(500) = 1$  and angle (5100) = 30°, then

15  $L(510) = L(500) / \cosine(30^\circ) = 1.0 / 0.866$

$L(510) = 1.155$ , or for

$L(500) = 1$  and angle (5200) = 45°, then

$L(520) = L(500) / \cosine(45^\circ) = 1.0 / 0.707$

$L(520) = 1.414$ ; and

20 for rotations of 30 to 45 degrees from the  
horizontal axis of the screen,

$\cosine(\theta) = L(501) / L(\theta)$  , so that for

$L(501) = 1$  and angle (5300) = 30°, then

$$L(530) = L(501) / \cosine (30^\circ) = 1.0 / 0.866$$

$$L(530) = 1.155, \text{ or for}$$

$$L(501) = 1 \text{ and angle } (5201) = 45^\circ, \text{ then}$$

$$L(520) = L(501) / \cosine (45^\circ) = 1.0 / 0.707$$

5       $L(520) = 1.414.$

The lenticular lenses tend to project a majority of the available light directly in front of the center portion of the screen where the viewer's eye is normally located. As the viewer moves about, the screen  
10 brightness is observed to roll-off. For the rotated dark-stripe structure of the present invention, this roll-off will be more pronounced along the diagonals from corner-to-corner of the screen. Although this diagonal roll-off is no more objectionable than the vertical and  
15 horizontal roll-off in conventional screens, the optimization of the vertical and horizontal components is no longer preserved to maintain the original viewing angles. The lenticular lens elements 60-65 and 600-605 shown in FIGURES 6a and 6b can be shaped to maintain the  
20 traditional brightness roll-off relative to the vertical and horizontal screen axes.

FIGURE 7 is a drawing of a rear-screen projection display, which uses the rotated dark-stripe screen of the present invention. The projector is housed in a free-

standing cabinet 70 and includes a projection engine 72, a relative large turning mirror 73, and the rotated black-strip rear-projection screen 71 of the present invention. The engine 72 can use any pixelated technology, although  
5 the example shown is for a digital micromirror device (DMD) projector. The engine 72 is located in the lower portion of the cabinet 70 and uses a single DMD 724 to modulate the light. This particular configuration of the engine 720 is comprised of a light source 720, which emits  
10 white light along a first light path, through a motor-driven rotating color filter wheel 721, which provides sequential red-green-blue (R-G-B) light. This sequential light is collected by an integrating rod 722 and passed through a condensing lens 723 where it is sized to fit the  
15 aperture of a total-internal-reflective (TIR) prism 725. The light is reflected off an internal surface of the TIR prism, on to the reflective mirrors of the DMD 724 where it is modulated and projected back through the TIR prism 725 along a second light path, through a projection lens 726  
20 and projected 741 (shaded area) on to the rather large turning mirror 73 positioned diagonally along the upper back surface of the cabinet 70, as shown. This sequential R-G-B light is then reflected 751 (shaded area) off the turning mirror 73 through the rotated dark-stripe screen  
25 71 for viewing by an observer. This shows one

configuration of one type engine that can be used with the screen of the present invention. Other DMD engine may not involve a TIR prism and/or an integrating rod. Other engines technologies, such as LCD, are also applicable, as  
5 are projectors using two or three spatial light modulators.

Typical pixel pitch at the screen for a projected image in a DMD rear-projection system is about 1.0 mm based on the projection lens 726 having a magnification of  
10 72x and a 57-inch diagonal image with 16:9 aspect ratio. This corresponds to an effective pitch of 1.4 mm for the rotated dark-stripe screen of the present invention. The margin against moiré fringes will become more critical as the pixels become smaller relative to the black stripe  
15 pitch in future projection systems.

The dark-stripe rear-projection screen 71 is that of the present invention, where the dark-stripe structure is rotated  $45 \pm 15$  degrees relative to the displayed pixels and/or the axes of the screen. The backside of the  
20 screen, where the projected image enters, consists of a layer of small lenticular lens elements 710. The dark-stripe structure is fabricated on the opposite surface (from the lens elements) of the lenticular layer and consists of diagonal black stripes 711 separated by  
25 transparent (clear) stripes 712. In this case the dark-



stripe structure is rotated  $45 \pm 15$  degrees relative to the displayed pixels. Next, a diffusion layer (not shown) is fabricated on top of the rotated dark-stripe layer to diffuse 752 the light 751, coming through the transparent stripes 712, across the entire screen. Finally a hard coating layer is applied on the outside surface of the screen for protection purposes.

In operation, the projector presents sequential R-G-B images to the screen 71 at a rate sufficient that the eye integrates the image to provide a high-performance color picture. The rotated black stripes 711 tend to make the screen look dark to the viewer while still letting light pass through it. This provides adequate picture contrast for viewing in a room with ordinary lighting conditions.

Where desirable, the lenticular lens elements can be shaped to cause the brightness roll-off in the screen to occur in the vertical and horizontal directions. This screen 71 improves the margin for preventing moiré patterns from occurring by effectively increasing the pixel pitch to screen structure pitch ratio by a factor of up to 1.41.

While the present invention has thus far been discussed in terms of the preferred method of aligning the dark stripe structures of the display screen diagonally across a pixelated image formed by vertical

columns and horizontal rows of pixels, it should be understood that an alternate embodiment provides vertical or horizontal—from the viewer's perspective—dark stripe structures to prevent or reduce the moiré effect when an  
5 image formed by a staggered array of pixels is projected. Figures 8 and 9 show such arrangements.

In Figure 8, an array of diamond-shaped pixels 80 is provided. The diamond-shaped pixels 80 are arranged in an array such that each pixel is offset in the horizontal  
10 direction from the pixels in the rows immediately above and below. A portion of the display screen 82 is superimposed on the array of diamond-shaped pixels 80. As in prior embodiments, the display screen is comprised of alternating clear 83 and dark 84 stripe structures  
15 arranged at a rate of at least twice the horizontal pixel resolution. As in the previous embodiments, diagonal relationship between the dark screen structures 84 and the diagonal pixels tends to reduce the moiré effect. While the embodiment of Figure 8 reduces the moiré  
20 effect, the diagonal pixels often produce noticeable jagged edges on vertical lines and therefore are often less desirable than the typical orthogonal array of pixels shown in Figures 5a and 5b.

In Figure 9, a staggered array of pixels is used.  
25 The staggered array of pixels 90 is comprised of rows of

rectangular pixels, each row offset in the horizontal direction from the rows immediately above and below. A portion of the display screen 92 is superimposed on the array of diamond-shaped pixels 90. As in prior

5   embodiments, the display screen is comprised of alternating clear 93 and dark 94 stripe structures arranged at a rate of at least twice the horizontal pixel resolution. As in the previous embodiments, diagonal

10   relationship between the dark screen structures 94 and the diagonal pixels tends to reduce the moiré effect. While the embodiment of Figure 9 reduces the moiré effect, the diagonal pixels often produce noticeable jagged edges on vertical lines and therefore are often less desirable than the typical orthogonal array of

15   pixels shown in Figures 5a and 5b.

The embodiments shown in Figures 8 and 9 each provide pixel arrays with strong diagonal orientations. These pixel arrays form diagonal groups of pixels having abutting sides—in contrast with traditional orthogonal

20   arrays in which diagonal pixels merely touch at the corners. By orienting the dark-structures of the display screen at an angle of  $45 \pm 15$  degrees relative to the diagonal groups of pixels having abutting sides the moiré effect is reduced.

While the present invention has been described in the context of preferred embodiments, it will be apparent to those skilled in the art that the present invention may be modified in numerous ways and may assume embodiments other  
5 than that specifically set out and described above. Accordingly, it is intended by the appended claims to cover all modifications of the invention that fall within the true spirit and scope of the invention.